



> The earth exerts a force on the moon and vice versa, even though they are 240,000 miles apart

> Likewise, two charged objects located far apart exert forces on each other too

- and the moon feels the effect of this field
- > Masses feel forces in gravitational fields
- > Similarly, a charge creates an electric field that fills all space
- > Any other charge in that field will feel a force
- > Stationary charges create electric fields that fill all space
- > Other charges will feel forces in these electric fields

Think of the electric field as a real physical entity!

Electric Field

How can they do this if they are not in physical contact?

> In the case of the earth/moon system, we say that the earth fills all space with a gravitational field,



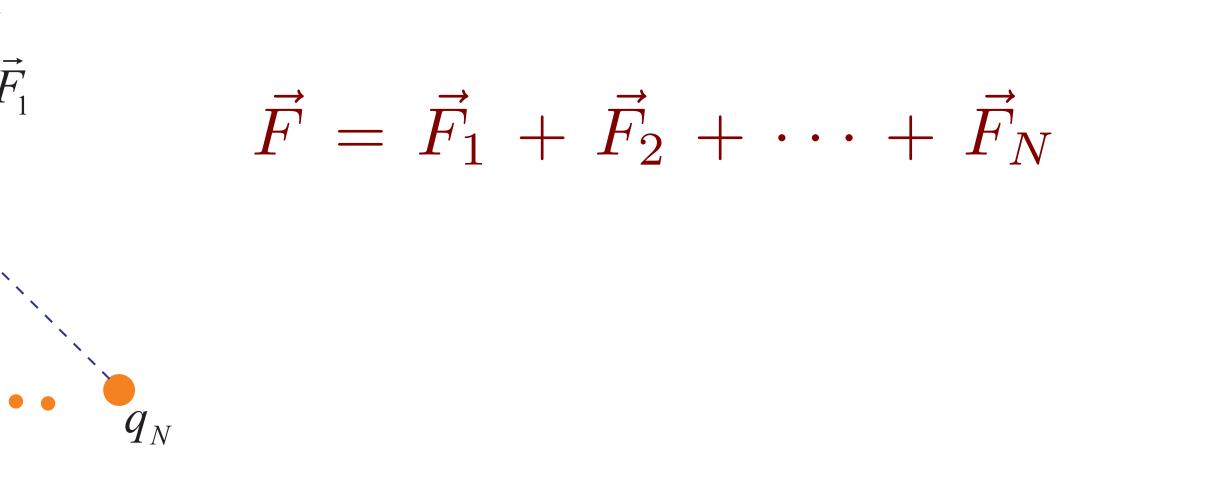


> When we solved the Coulomb Law problems we added up the (vector) forces from charges $q_1, q_2, \dots q_N$ acting on a certain charge q_0

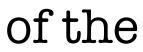
>Now reach one of these individual forces (and hence the sum of those forces) is proportional to the charge q_0

>If in each of those problems we divided the net force by the charge q_0 we would get a force per unit charge at the location of q_0 q_0 >This quantity (which is a vector, since force is a vector) would depend on the values and locations of the charges $q_1, q_2, \dots q_N$

Electric Field

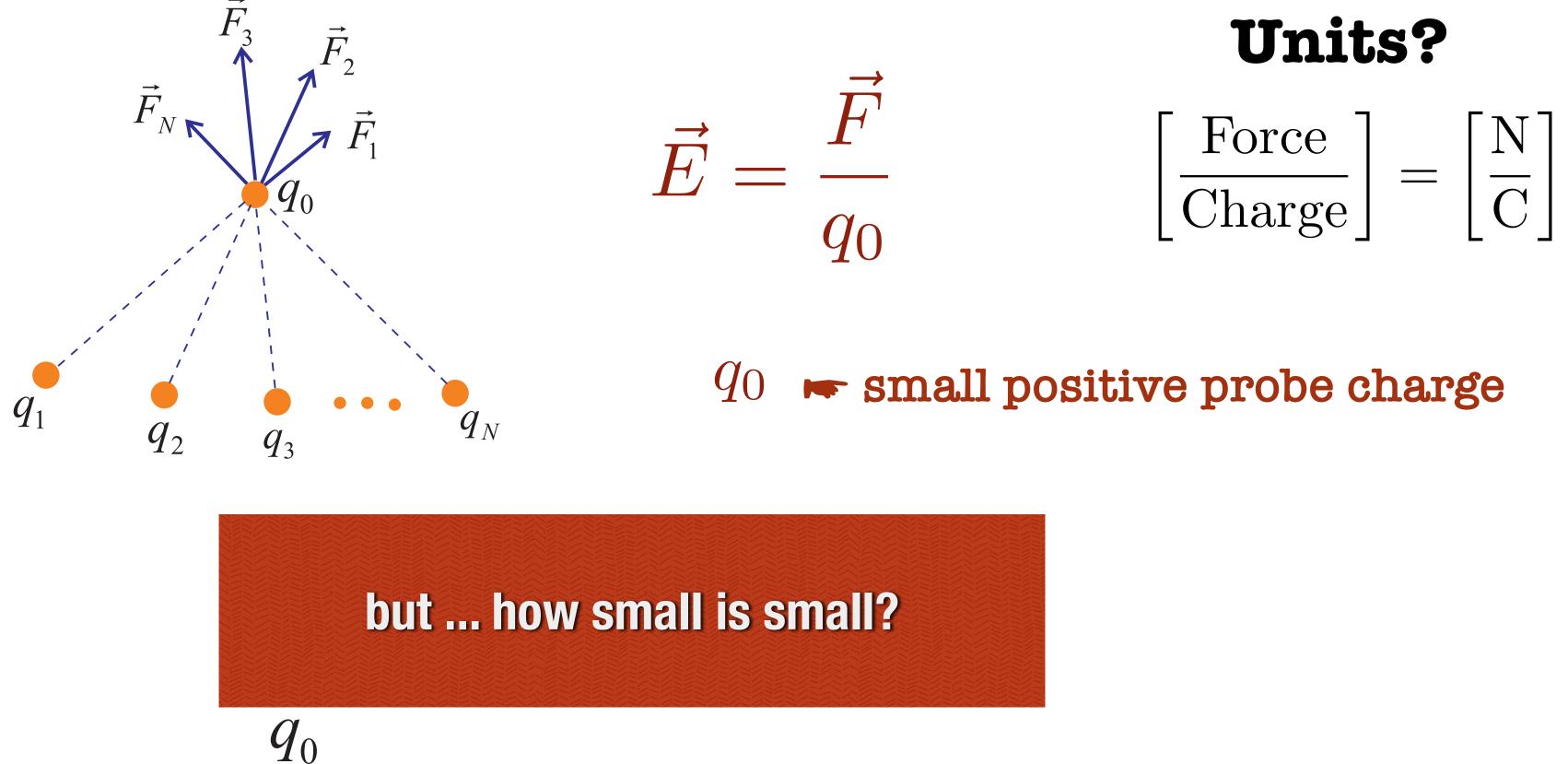








> So real a given configuration of charges $q_1, q_2, ..., q_N$ gives rise to an electric field

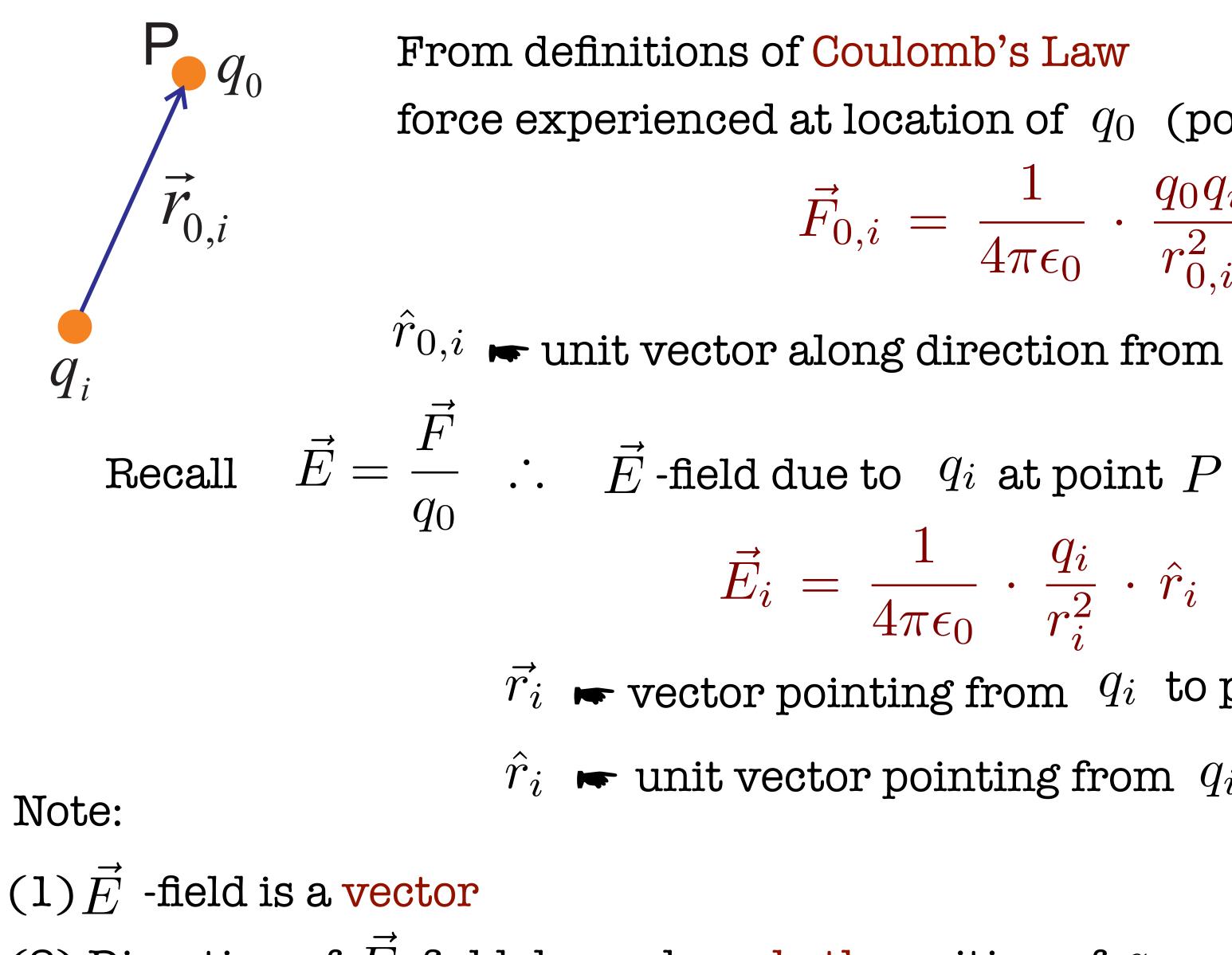


> When we use this equation we mean that after we put q_0 in place all the little charges $q_1, q_2, \dots q_N$ are in the same places they were when we deduced the value of E from their values and positions!

Electric Field



(i) E-field due to a single charge q_i



force experienced at location of q_0 (point P) $\vec{F}_{0,i} = \frac{1}{4\pi\epsilon_0} \cdot \frac{q_0 q_i}{r_0^2} \cdot \hat{r}_{0,i}$

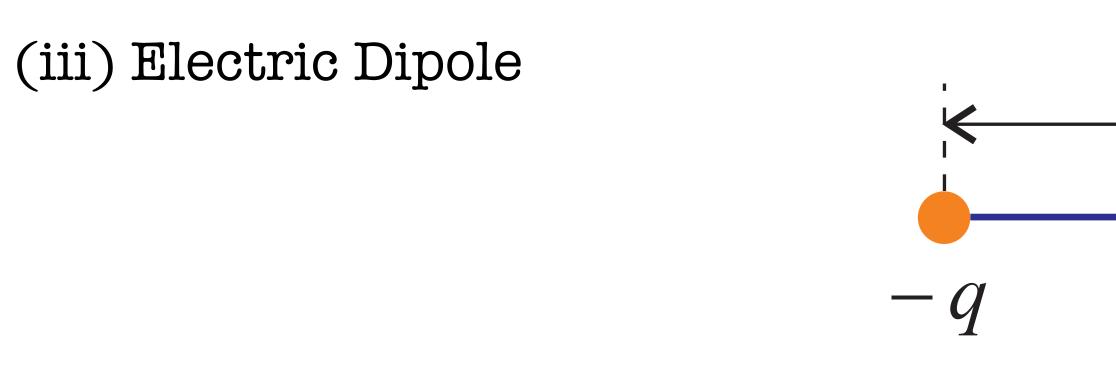
 $\hat{r}_{0,i}$ reprint which we can be along direction from charge q_i to q_0

 $\vec{E}_i = \frac{1}{4\pi\epsilon_0} \cdot \frac{q_i}{r_i^2} \cdot \hat{r}_i$ $\vec{r_i}$ revector pointing from q_i to point P \hat{r}_i is unit vector pointing from q_i to point P

(2) Direction of \vec{E} -field depends on both position of q_i and its sign

(ii) \vec{E} -field due to system of charges: Principle of Superposition

In a system with N charges rackstriant total E-field due to all charges vector sum of \vec{E} -field due to individual charges i.e. $rac{\vec{E}} =$



System of equal and opposite charges separated by a distance dElectric Dipole Moment $rac{\vec{p}}{\vec{p}} = q\vec{d} = qd\hat{d}$ p = qd

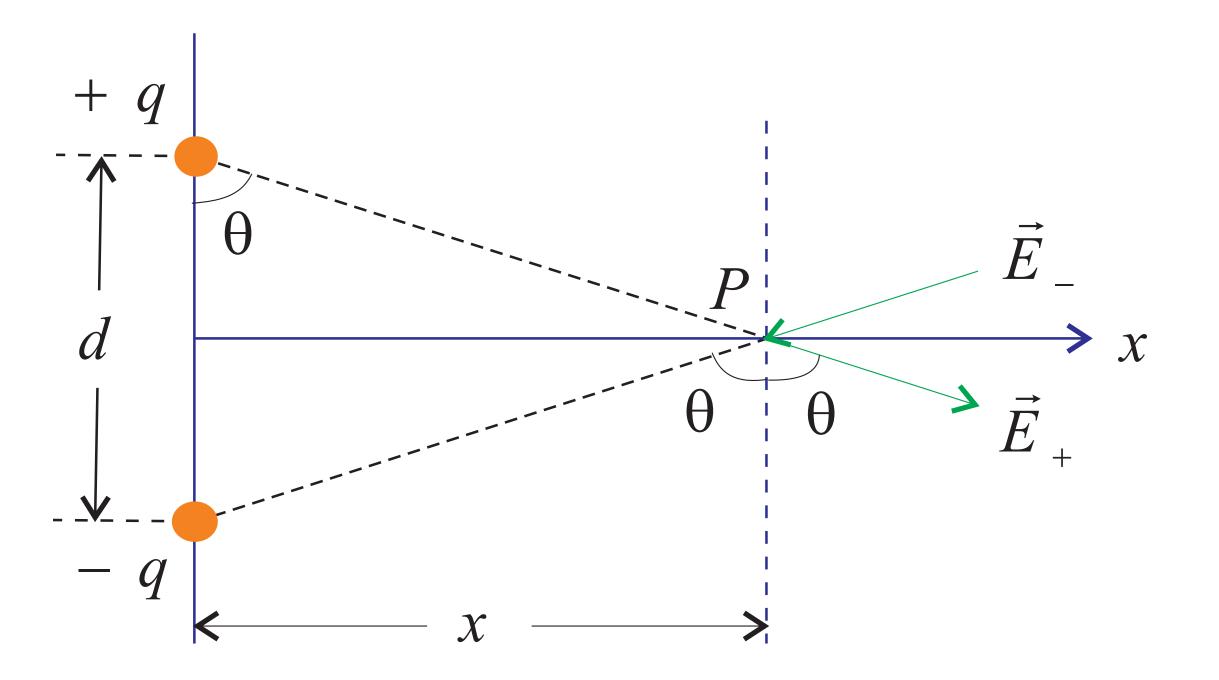
$$\sum_{i} \vec{E}_{i} = \frac{1}{4\pi\epsilon_{0}} \sum_{i} \frac{q_{i}}{r_{i}^{2}} \hat{r}_{i}$$

$$d \longrightarrow$$

$$\vec{d} \rightarrow$$

$$\vec{d} + q$$

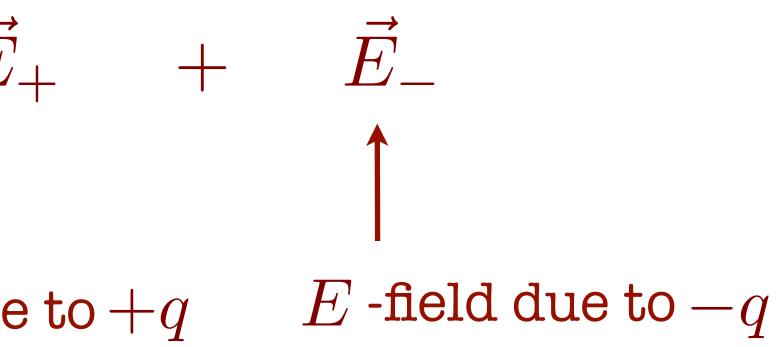
Example: \vec{E} due to dipole along *x*-axis



Consider point P at distance x along perpendicular axis of dipole \vec{p}

$$\vec{E} = \vec{E}$$

 \vec{E}

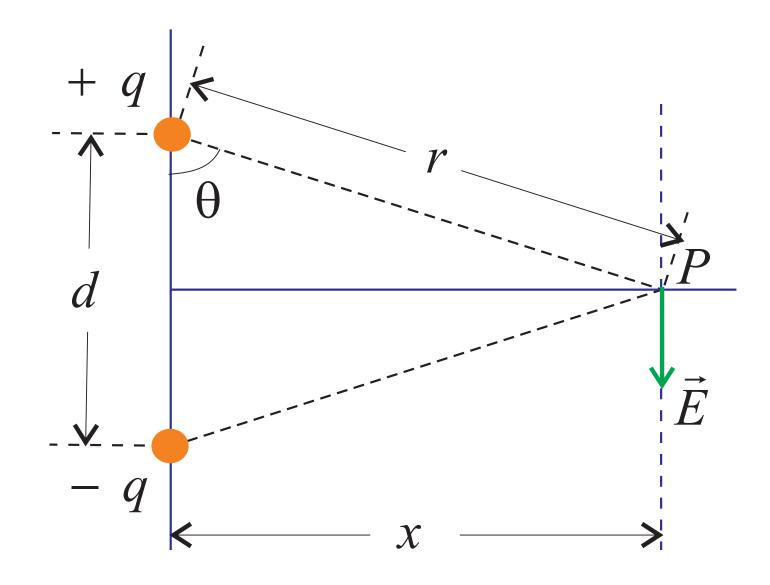


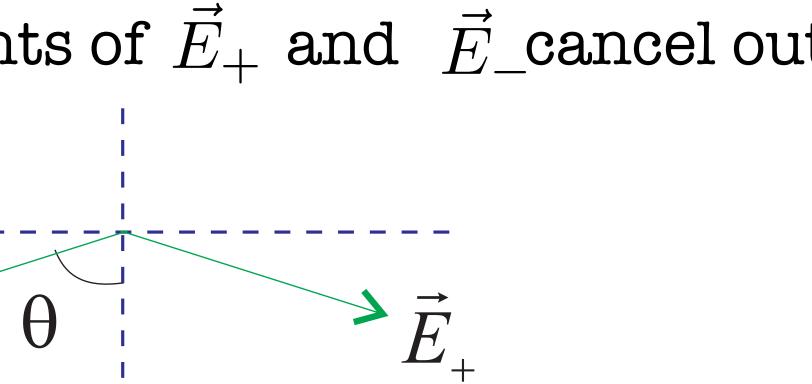
Notice: Horizontal \vec{E} -field components of \vec{E}_+ and \vec{E}_- cancel out

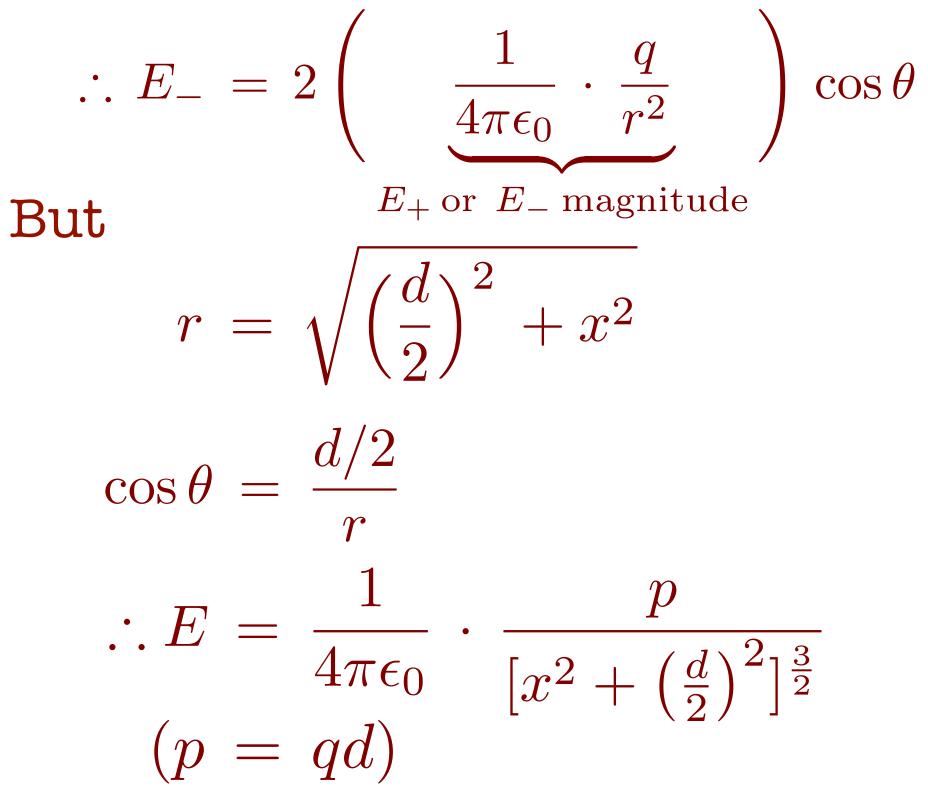
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 \therefore Net \vec{E} points along axis parallel but opposite to dipole moment vector Magnitude of \vec{E} -field = $2E_+ \cos \theta$







Special case $rac{}$ When $x \gg d$ $\left[x^{2} + \left(\frac{d}{2}\right)^{2}\right]$

> Binomial Approximation

 \vec{E} – field of dipo

> Compare with $\frac{1}{r^2}$ \vec{E} -field for single charge

> Result also valid for point P along any axis with respect to dipole

$$\frac{3}{2} = x^3 \left[1 + \left(\frac{d}{2x}\right)^2 \right]^{\frac{3}{2}}$$

 $(1+y)^n \approx 1+ny$ if $y \ll 1$

ple
$$\simeq \frac{1}{4\pi\epsilon_0} \cdot \frac{p}{x^3} \propto \frac{1}{x^3}$$

Conventions

1. Start on positive charges and end on negative charges

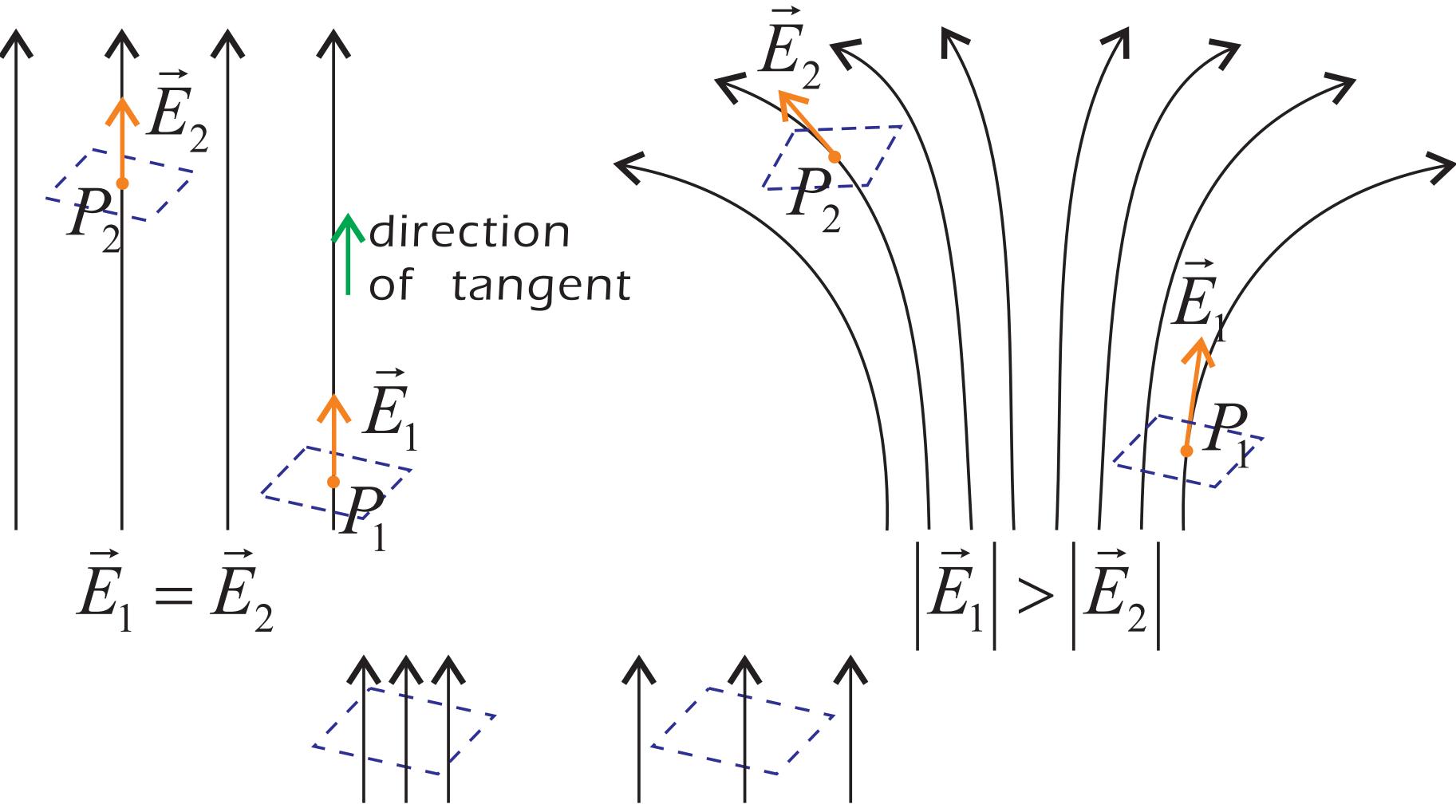
2. Direction of E-field at any point is given by tangent of E-field line

3. Magnitude of E-field at any point proportional to number of E-field lines per unit area perpendicular to lines

Electric Field Lines

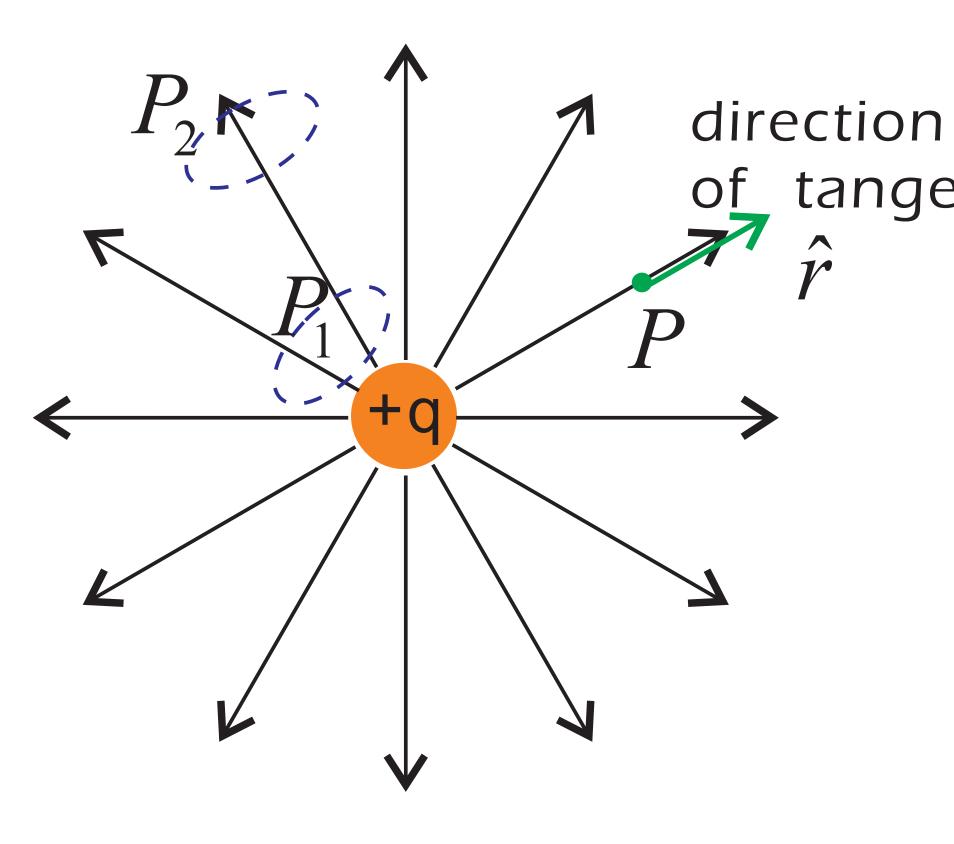
To visualize electric field we can use a graphical tool called electric field lines

Uniform E-field

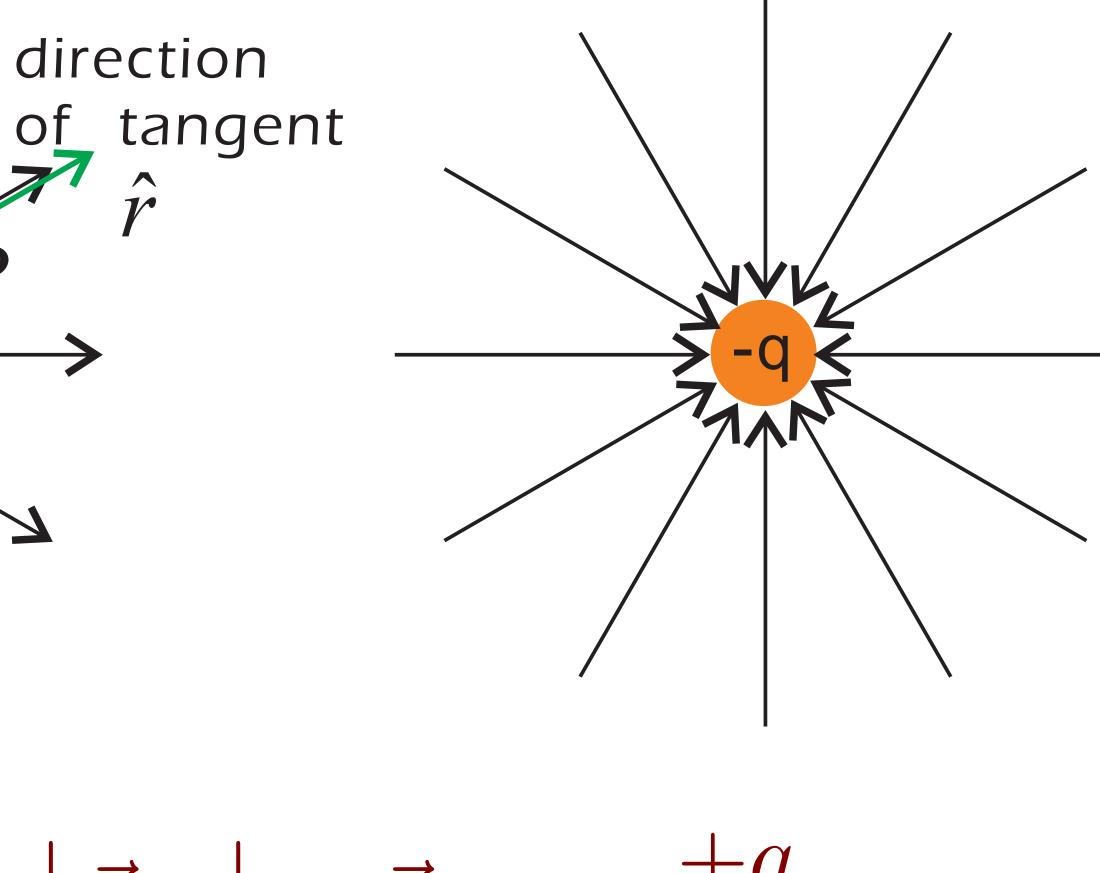


Non-uniform E-field

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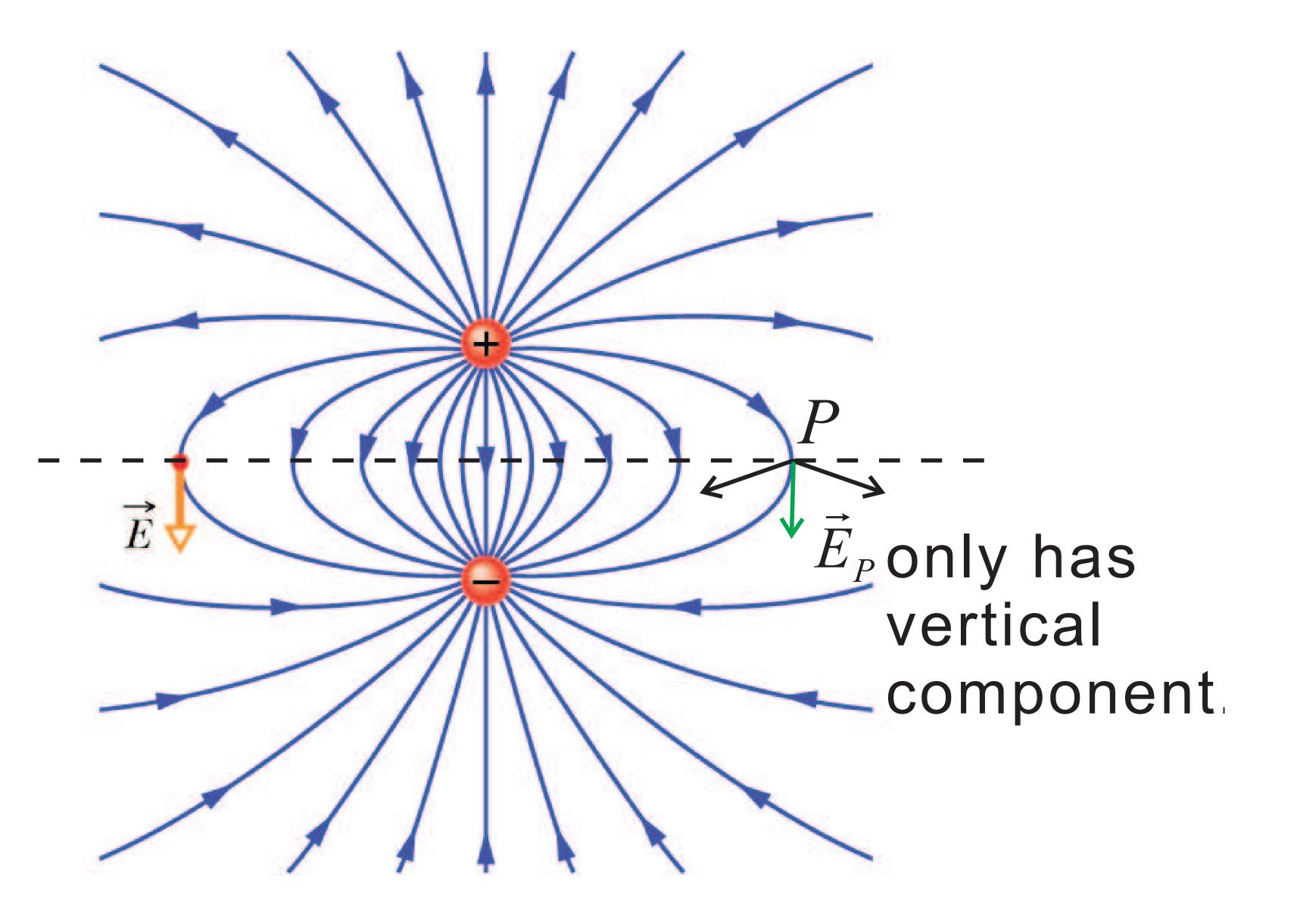


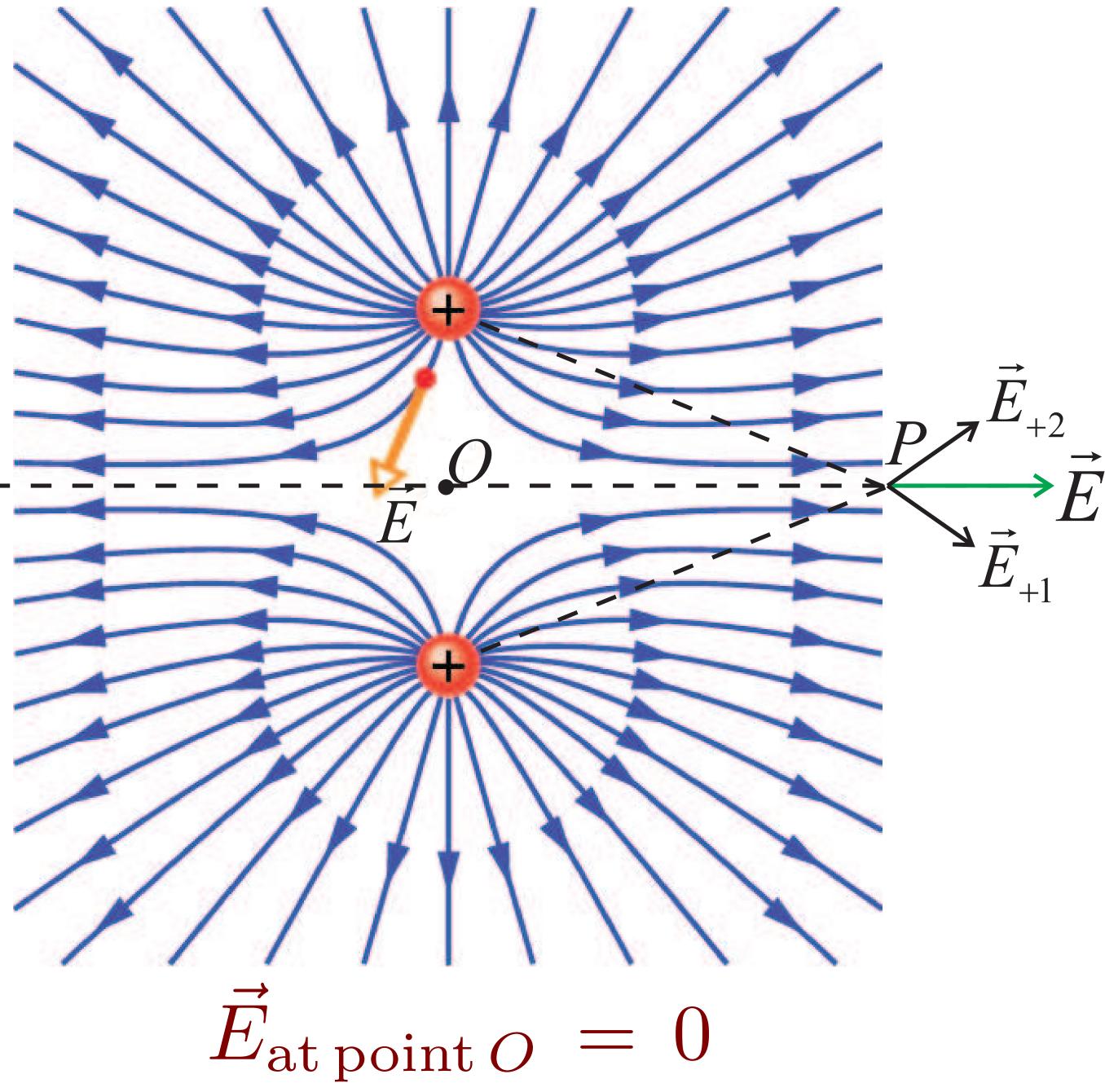




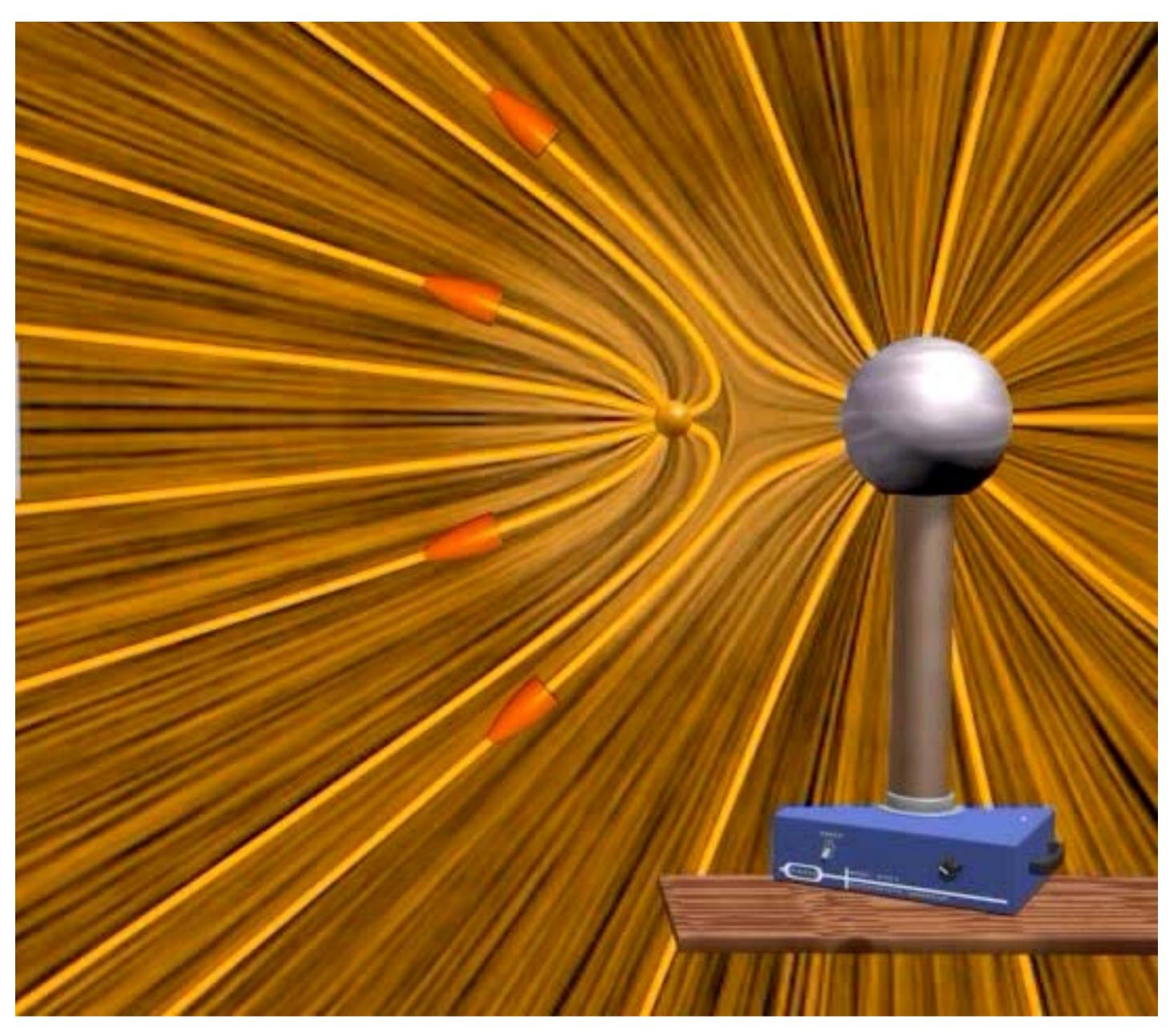








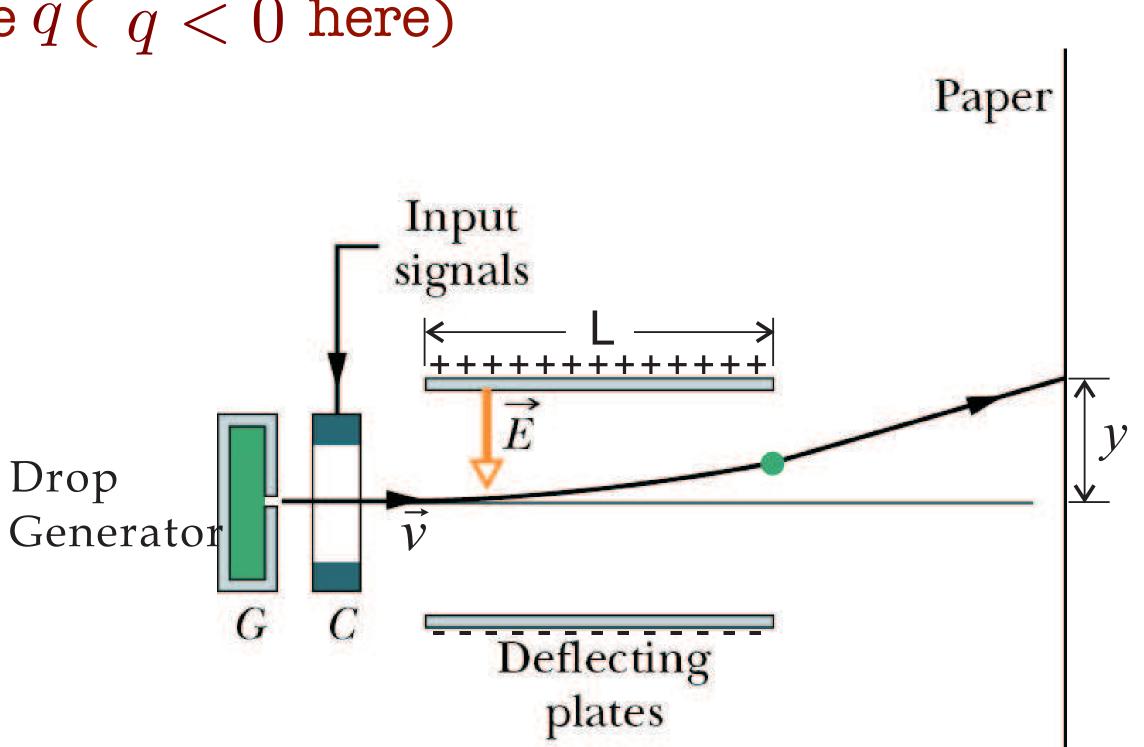
This is not a probe charge



Point Charge in E-field

When we place a charge q in an E-field \vec{E} , force experienced by charge is

Applications - Ink-jet printer, TV cathode ray tube Example Ink particle has mass m & charge q (q < 0 here)

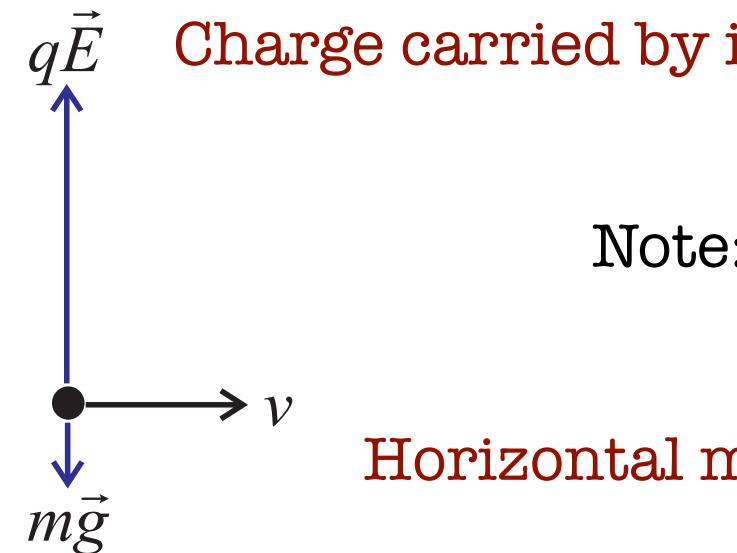


- $\vec{F} = q\vec{E} = m\vec{a}$

Assume that mass of inkdrop is small, what's deflection of charge?



Solution \blacksquare



Vertical mot

 $\therefore \text{ Net force } = -|q|E$ $\therefore a = -\frac{|q|E}{m}$

Vertical distance

Charge carried by inkdrop is negative $\blacksquare q < 0$

- Note: $q\vec{E}$ points in opposite direction of \vec{E}
- Horizontal motion \blacksquare Net force = 0

$$\therefore L = vt$$
tion 🖛 $|qec{E}| \gg |mec{g}|$ q is negative

 \therefore Net force = -|q|E = ma rewton's 2nd Law

travelled
$$raw y = \frac{1}{2} a t^2$$

Conductors and insulators

Charges move through some materials more easily than others:

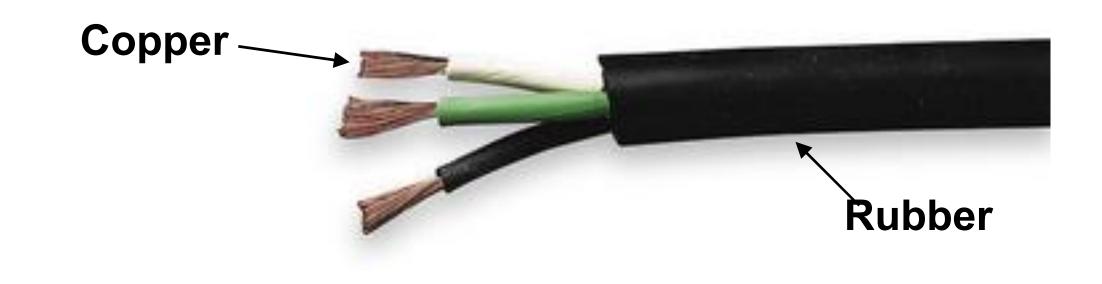
Charge moves easily: Conductor

i.e. copper, silver, aluminum (metals)

Charge can't move: Insulator

i.e. wood, paper, rubber, plastic,

Charge can stick on the surface of insulators, but it doesn't really move



Electrical Wire

- > They can "break free" and move through the material > These are called **conduction electrons** -5 C

Let's say the object on the left starts out with a charge of -5 C, and the object on the right starts out with +13 C

Electrons will continue to flow until the charge on each object is....?

And, each must end up with a charge of +4C, since the total (+8C) must remain constant!

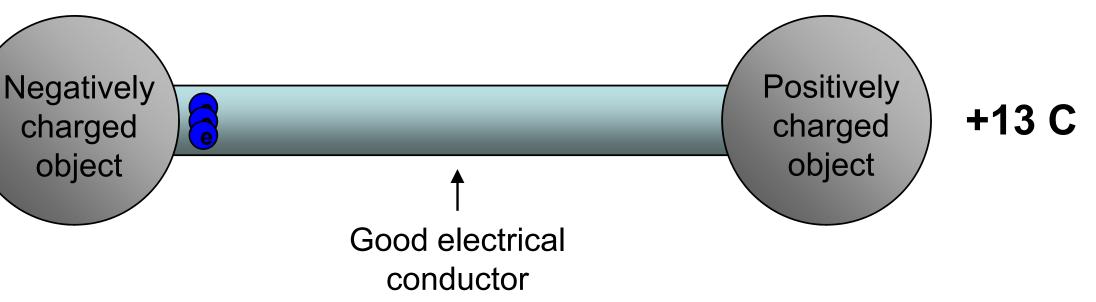
Electrons can "flow" through a good conductor

There would be no charge flow if the bridge above was an insulator

What determines whether a material is a good conductor o insulator?

➡ Ultimately, it's the **atomic structure**

 \succ The outer most electrons (valence electrons) in an atom are more weakly bound to the nucleus

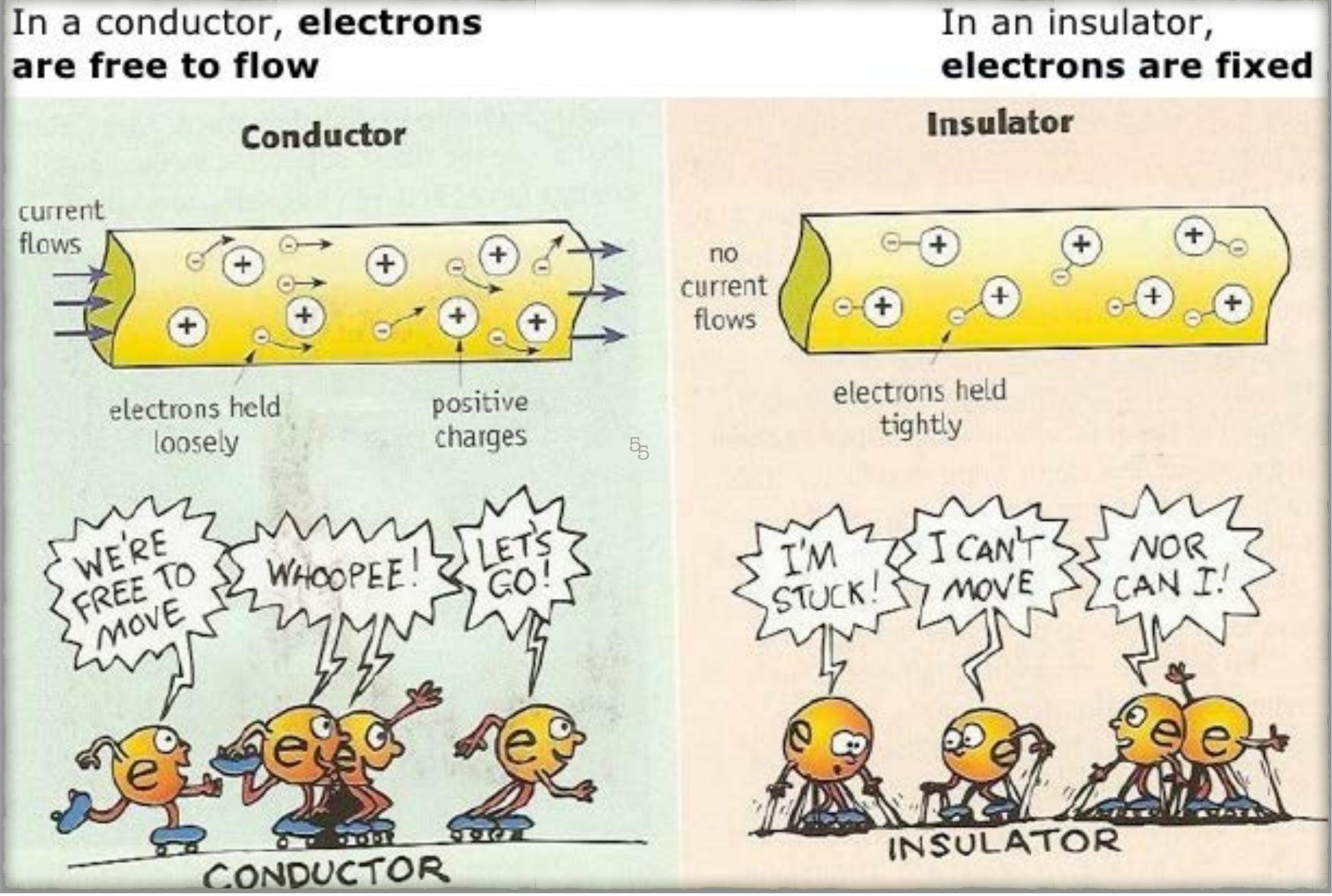








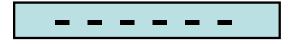






Charging by Contact

> Touching a metal sphere with a negatively charged rod can give the sphere a negative charge

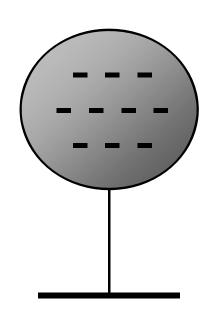


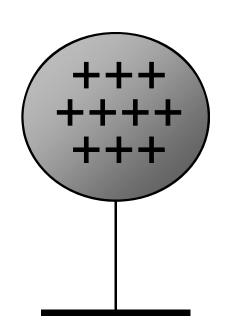
> Similarly, if we started with a positively charged rod:



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This is charging by contact



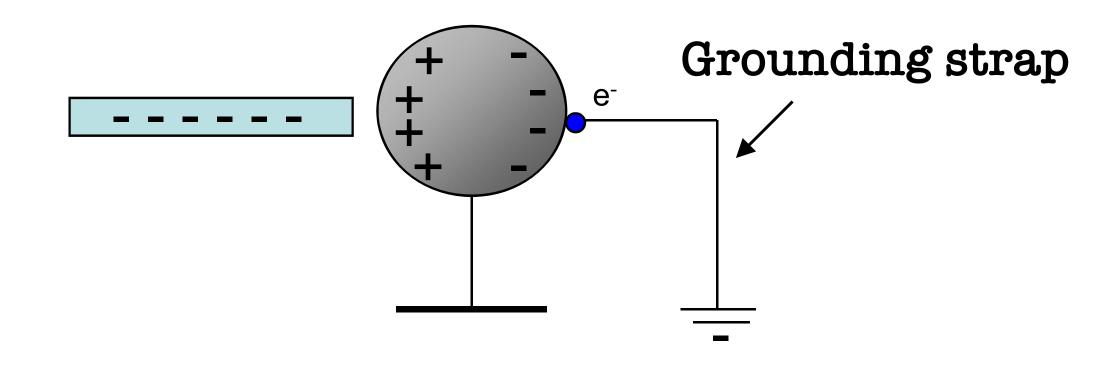


Charging by Induction

We can also charge a conductor without actually touching it

Bring a negatively charged rod close to the surface of an electrically neutral metal sphere

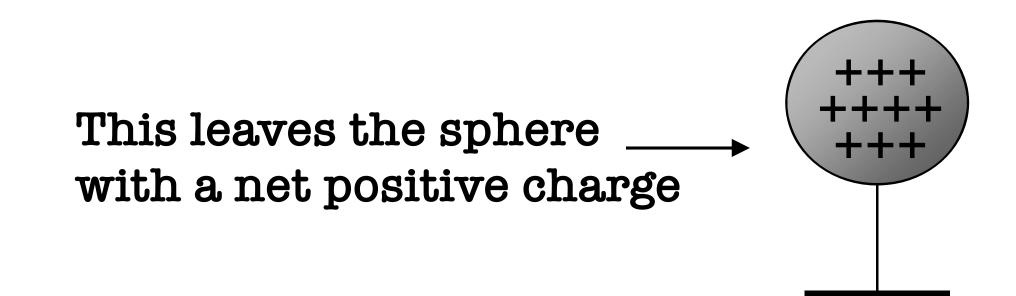
Now attach a metal wire between the sphere and ground



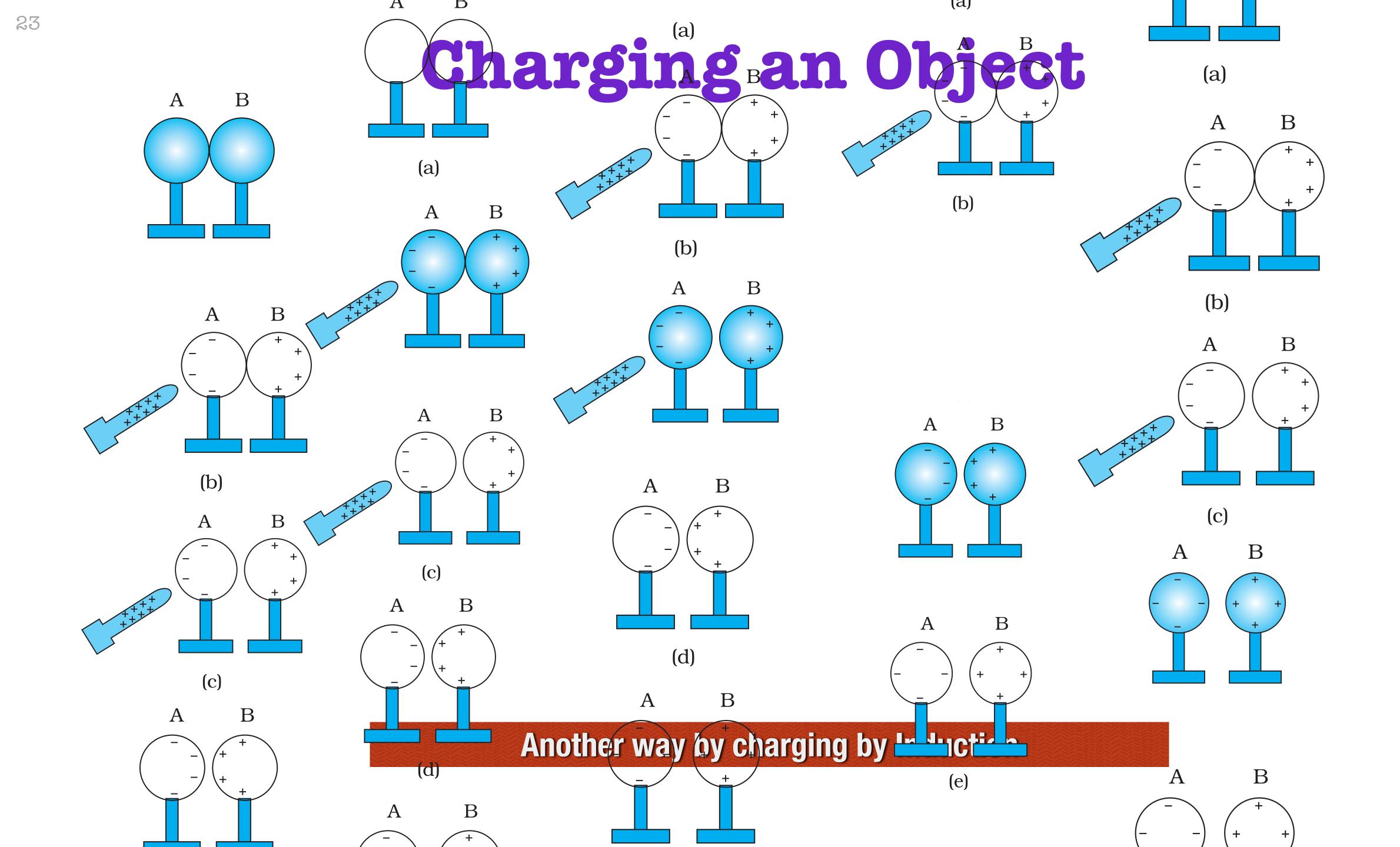
The electrons travel down the strap to ground

Charging an Object

The free charges separate on the sphere's surface

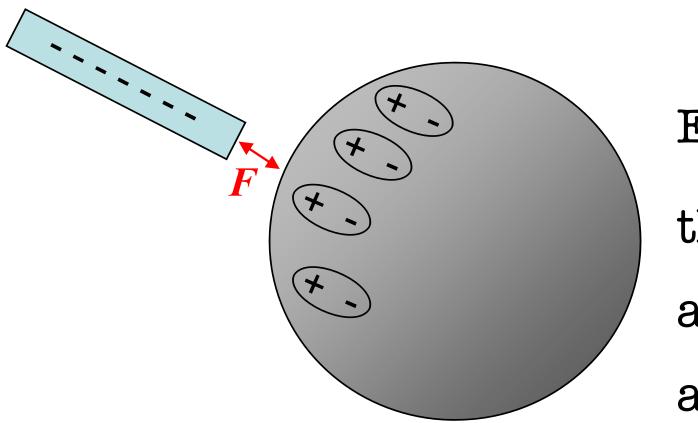


This is charging by Induction



> Charging by induction doesn't work for insulators, since the charge can't move through the material or down the grounding strap

> Bring a negatively charged rod close to the surface of an insulating sphere



But it does have an effect....

Even though the electrons can't move through the insulator,

the positive and negative charge in each atom separates slightly

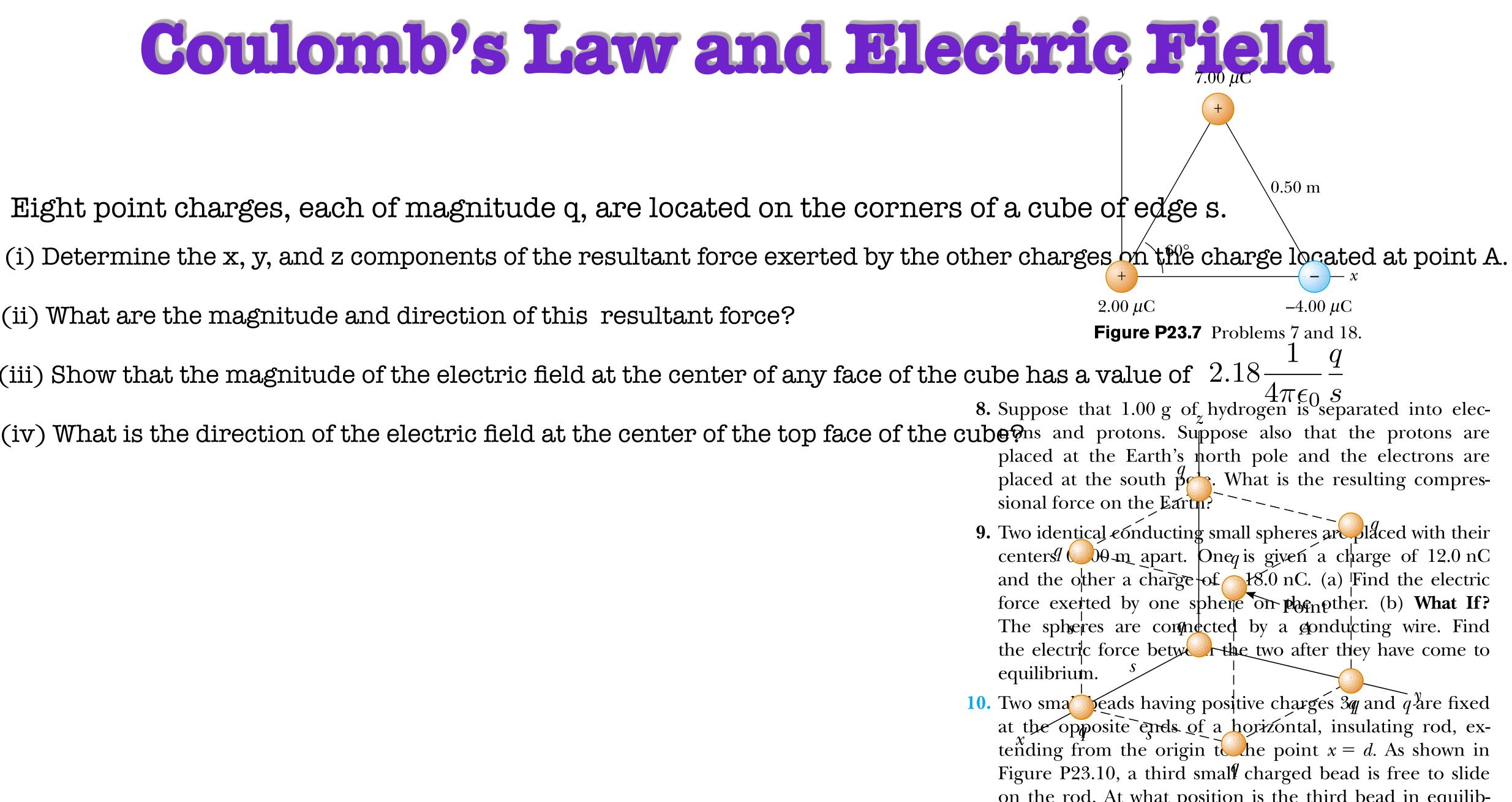
and forms dipoles, since the positive protons in the atoms are

attracted to the rod, and the negative electrons are repelled

This is called Polarization



Eight point charges, each of magnitude q, are located on the corners of a cube of edge s. (ii) What are the magnitude and direction of this resultant force? (iii) Show that the magnitude of the electric field at the center of any face of the cube has a value of ~2.18-



on the rod. At what position is the third bead in equilib-



Coulomb's Law and Electric Field

Solution (i)

- There are 7 terms that contribute
- * There are 3 charges a distance s away (along sides), 3 a distance $\sqrt{2s}$ away (face diagonals), and one charge a distance $\sqrt{3s}$ away (body diagonal)
- * By symmetry, the x, y and z components of the electric force must be equal * Thus, we only need to calculate one component of the total force on the charge of ineterest Point * We will choose the coordinate system as indicated in Figure, and calculate the y component of the force.



Coulomb's Law and Hereit Externa Coulomb's Law and Solution $3 \text{ are } \sqrt{2s}$ away (face diagonals) and $\sin \theta =$

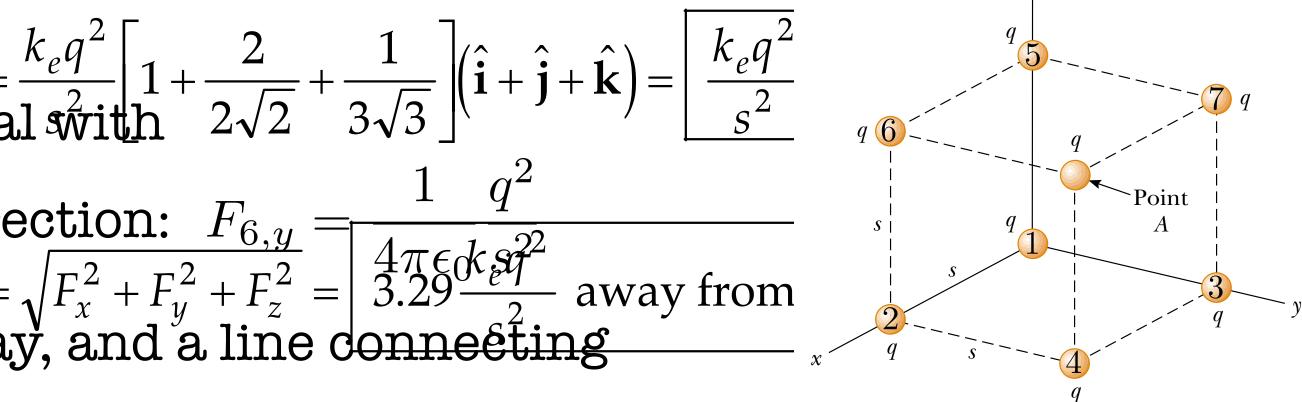
P23.69

(a)

* We can already see that several charges will not give a y component strees torce at all flust from symmetry - charges 3, 4 and 7 Symmetry - Charges 0, 4 and 7 $\mathbf{F} = \frac{k_e q^2}{2} \left[1 + \frac{2}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right] (\hat{\mathbf{i}} + \hat{\mathbf{j}} + \hat{\mathbf{k}}) = \left[\frac{k_e q^2}{s^2} \right]$ This leaves only charges 1, 2, 5, and 6 to deal with Charge 6 will give a force purely in the y direction: $F_{6,y} = \frac{1}{4\pi\epsilon_0 k_s q^2} = \frac{4\pi\epsilon_0 k_s q^2}{3.29 \frac{4\pi\epsilon_0 k_s q^2}{2}}$ away from the y direction: $F_{6,y} = \frac{4\pi\epsilon_0 k_s q^2}{3.29 \frac{4\pi\epsilon_0 k_s q^2}{2}}$ away from the y direction is $s\sqrt{2}$ away, and a line connecting Point these charges with the charges of interest make antapaten from the with face due to symmetry, opposite face contributes the y-axis in both cases * Hence, noting that $\cos \theta = 1/\sqrt{2}$ we obtain $F_{2,y} = F_{5,y} = \frac{1}{4\pi\epsilon_0} \frac{q^{2\sqrt{r}}}{(s\sqrt{s_1})^2}$

There are 7 terms which contribute:

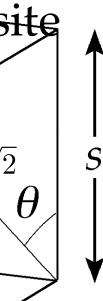




$$\frac{k_e q}{r^2} \sin \phi \text{ where } r = \sqrt{\left(\frac{s}{2}\right)^2 + \left(\frac{s}{2}\right)^2 + s^2} = \sqrt{1.5s} = 1.22s$$







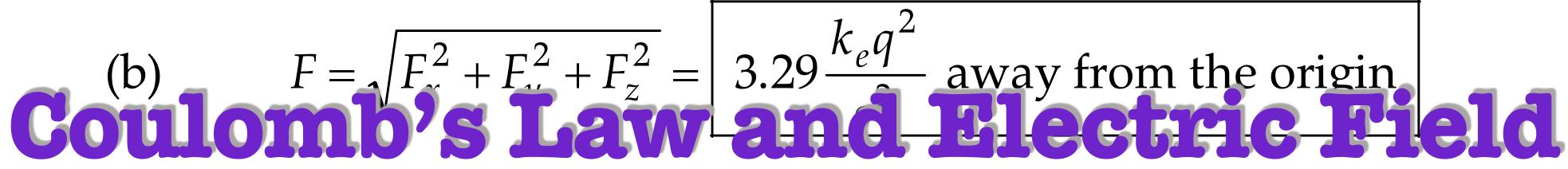
P23.70 (a) face contributes * Finally, we have charge 1 to deal with. * It is a distance $\sqrt{3}$ away² $\sin \phi$ where $r = \sqrt{\left(\frac{s}{2}\right)^2 + \left(\frac{s}{2}\right)^2 + s^2} = \sqrt{1.5s} = 1.22s$

* What is the y composite f_r of the force from charge $\frac{k_e qs}{r^3} = \frac{4}{(1\ 22)^3} \frac{k_e q}{s^2} = \frac{4}{2.18\sqrt{\frac{2}{2}}}$

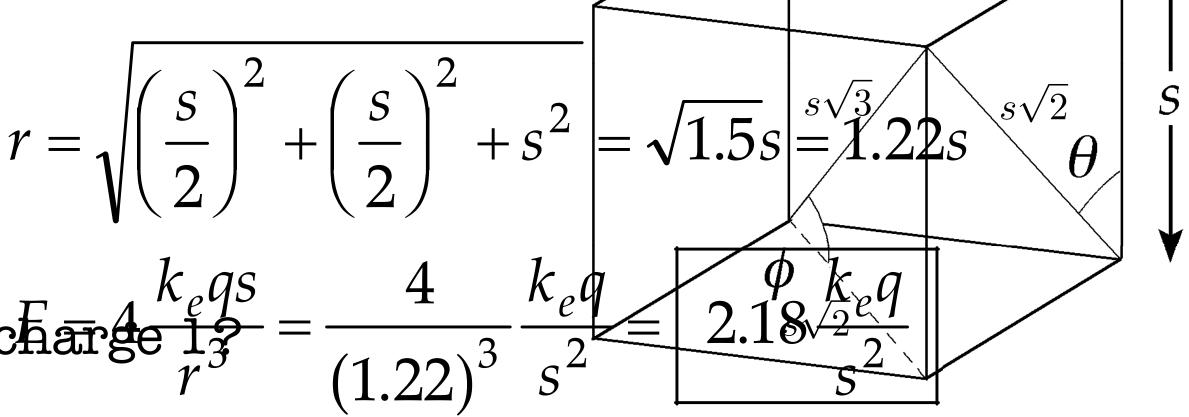
The direction is the **k** direction. (b)

* Now, we can find the component of of the force along the y direction:

$$F_{1,y} = F_{1,x-y} \cos \theta = F_{1,x-y} \frac{1}{\sqrt{2}} = F_1 \frac{\sqrt{2}}{\sqrt{3}} \frac{1}{\sqrt{2}} = F_1 \frac{1}{\sqrt{3}}$$



Zero contribution from the same face due to symmetry, opposite



First, we can find the component of the force in the x-y plane $F_{1,x-y} = F_1 \cos \phi = F_1 \frac{\sqrt{2}}{\sqrt{2}}$



Coulomb's Law and Electric Field

* Since we know charge 1 is a distance $s\sqrt{3}$ away, we can calculate the full force F_1 easily, and complete the expression for $F_{1,y}$ that is $F_{1,y} = \frac{1}{4\pi\epsilon_0} \frac{q^2}{(s\sqrt{3})^2} \frac{1}{\sqrt{3}} = \frac{1}{4\pi\epsilon_0} \frac{q^2}{s^2} \frac{1}{3\sqrt{3}}$ * Now we have the y component for the force from every charge; the net force in the y direction is just the sum of all those:

$$F_{y,\text{net}} = F_{1,y} + F_{2,y} + F_{5,y} + F_{6,y} = \frac{1}{4\pi\epsilon_0} \frac{q^2}{s^2} \left[1 + \frac{1}{2\sqrt{2}} + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right] = \frac{1}{4\pi\epsilon_0} \frac{q^2}{s^2} \left[1 + \frac{1}{\sqrt{2}} + \frac{1}{3\sqrt{3}} \right]$$

The force is then $\vec{F} = \frac{1}{4\pi\epsilon_0} \frac{q^2}{s^2} \left| 1 + \frac{1}{\sqrt{2}} + \frac{1}{3\sqrt{3}} \right| (\hat{i})$

* Since the problem is symmetric in the x, y, and z directions, all three components must be equivalent

$$\hat{i} + \hat{j} + \hat{k}) = 1.90 \frac{1}{4\pi\epsilon_0} \frac{q^2}{s^2} (\hat{i} + \hat{j} + \hat{k})$$





Coulomb's Law and Electric Field

contribute: Solution (ii) g sides) $F = \sqrt{F_x^2 + F_y^2 + F_z^2} = 3.29 \frac{1}{4\pi\epsilon_0} \frac{q^2}{s^2}$ awe face diagonals) and $\sin\theta = \frac{1}{\sqrt{2}} = \cos\theta$ dy diagonaly and contribution from the satThe opposite face contributes $\frac{q \sin \phi}{\pi \epsilon_0 r^2}$. $= \hat{\mathbf{s}} \text{All in all} \underbrace{F = \frac{q \ s}{k_e q^2 \pi \epsilon_0 r^3} = 2.18 \frac{1}{4\pi \epsilon_0} \frac{q}{s^2}}_{\mathbf{s}} \underbrace{\hat{\mathbf{s}}_{\mathbf{s}} \hat{\mathbf{s}}_{\mathbf{s}}}_{\mathbf{s}} = (\hat{\mathbf{s}} \hat{\mathbf{s}}_{\mathbf{s}} \hat{\mathbf{s}} \hat{$ ***** The direction is k

 $k a^2$

mg

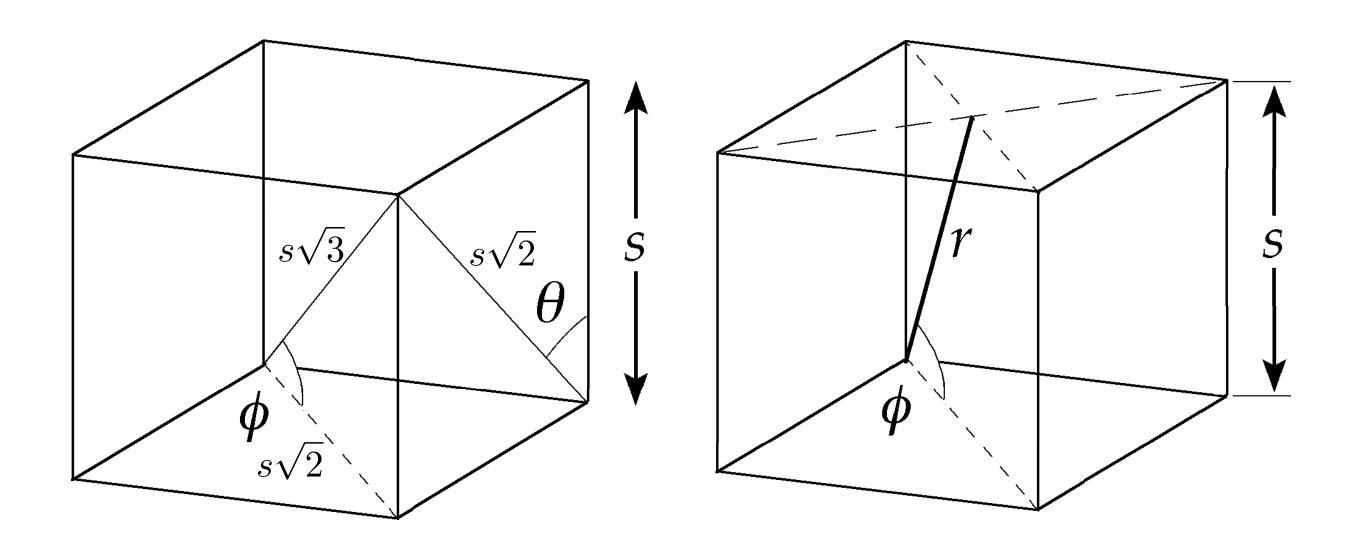


FIG. P23.69

nd $\sin \phi = s/r$



